

$$l_1 = 1 \mu$$

$$l_2 = 1,4 \mu$$

$$l_3 = 1,1 \mu$$

$$a_1 = 0,8 \mu$$

$$a_2 = 2a_3 = 1,3 \mu$$

$$F_1 = 40 \text{ kN}$$

$$F_2 = 20 \text{ kN}$$

$$F_3 = 30 \text{ kN}$$

$$q = 40 \text{ kN}/\mu$$

$$0 < \underline{I} < (l_1 + l_2 + l_3 - a_1 - a_2 - a_3)$$

$$N_z' = -q z \Big|_0^{(l_1 + l_2 + l_3 - a_1 - a_2 - a_3)} =$$

$$N_z'(l_1 + l_2 + l_3 - a_1 - a_2 - a_3) = -q(l_1 + l_2 + l_3 - a_1 - a_2 - a_3) =$$

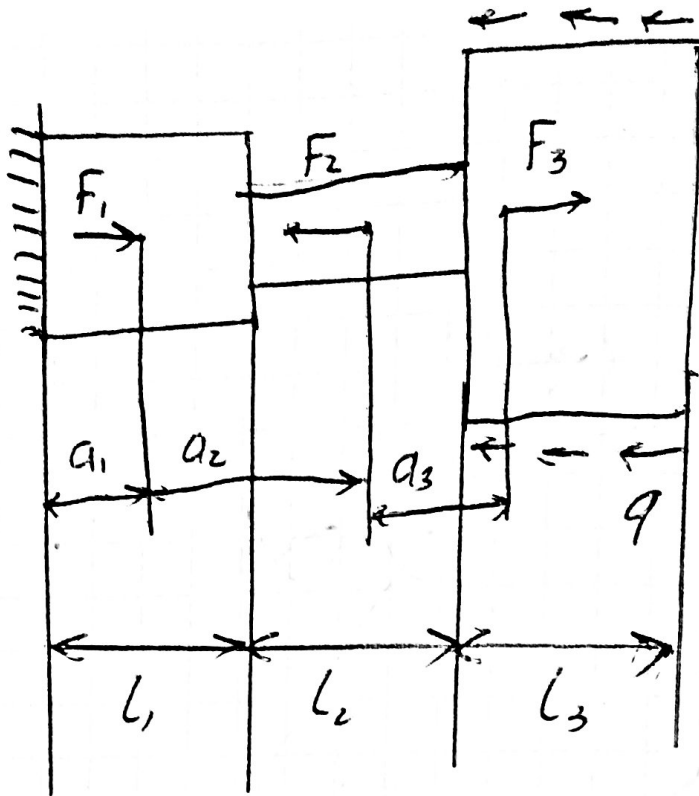
$$= -40(1 + 1,4 + 1,1 - 0,8 - 1,3 - \frac{1,3}{2}) = -30 \text{ kN}$$

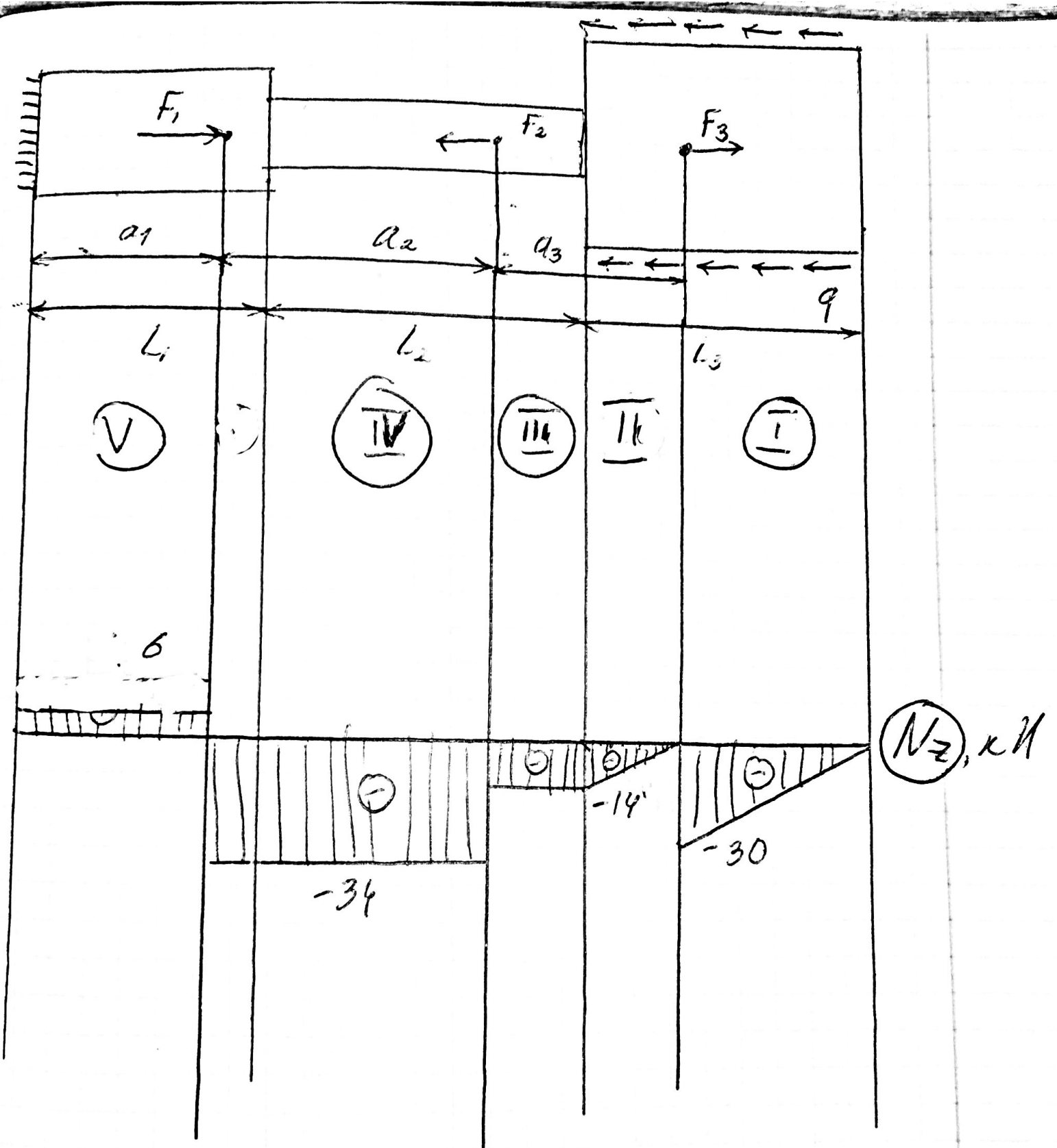
$$(l_1 + l_2 + l_3 - a_1 - a_2 - a_3) < \underline{II} < (l_3)$$

$$N_z'' = -q z + F_3 \Big|_{l_1 + l_2 + l_3 - a_1 - a_2 - a_3}^{l_3}$$

$$N_z''(l_1 + l_2 + l_3 - a_1 - a_2 - a_3) = -q(l_1 + l_2 + l_3 - a_1 - a_2 - a_3) +$$

$$+ F_3 = -30 + 30 = 0 \text{ kN}$$





$$N_z''(l_3 + \dots) = -q(l_3 + \dots) + F_3 = -40(1,1) + 30 = -14 \text{ kN}$$

$$L_3 < \textcircled{\text{III}} < (l_1 + l_2 + l_3 - a_1 - a_2)$$

$$N_z''' = -ql_3 + F_3 = -14 \text{ kN}$$

$$(l_1 + l_2 + l_3 - a_1 - a_2) < \textcircled{\text{IV}} < (l_2 + l_3 + l_1 - a_1)$$

$$N_z^{IV} = -ql_3 + F_3 - F_2 = -40 \cdot 1,1 + 30 - 20 = -34 \text{ kN}$$

$$(l_2 + l_3 + l_1 - a_1) < \textcircled{\text{V}} < (l_1 + l_2 + l_3)$$

$$N_z^V = -ql_3 + F_3 - F_2 + F_1 = -40 \cdot 1,1 + 30 - 20 + 40 = 6 \text{ kN}$$

$$a_1 = 0,6 \text{ м}$$

$$a_2 = 0,4 \text{ м}$$

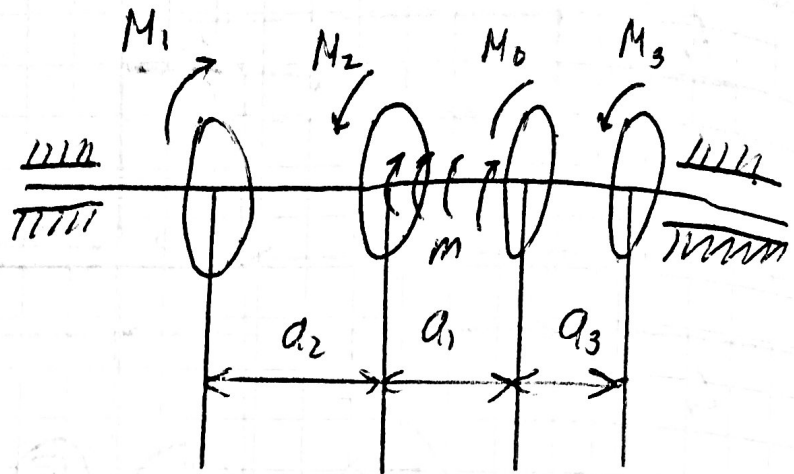
$$a_3 = 0,2 \text{ м}$$

$$M_1 = 2,2 \text{ кНм}$$

$$M_2 = 2,8 \text{ кНм}$$

$$M_3 = 3,0 \text{ кНм}$$

$$m = 10,0 \text{ кН/м}$$



Находим  $M_0$

$\sum M_z = 0$  - условие равновесия

$$M_1 - M_2 + m a_1 + M_0 - M_3 = 0$$

$$M_0 = M_3 + M_2 - M_1 - m a_1 = 3 + 2,8 - 2,2 - 10 \cdot 0,6 = -2,4 \text{ кНм}$$

Построение эпюры  $M_z$

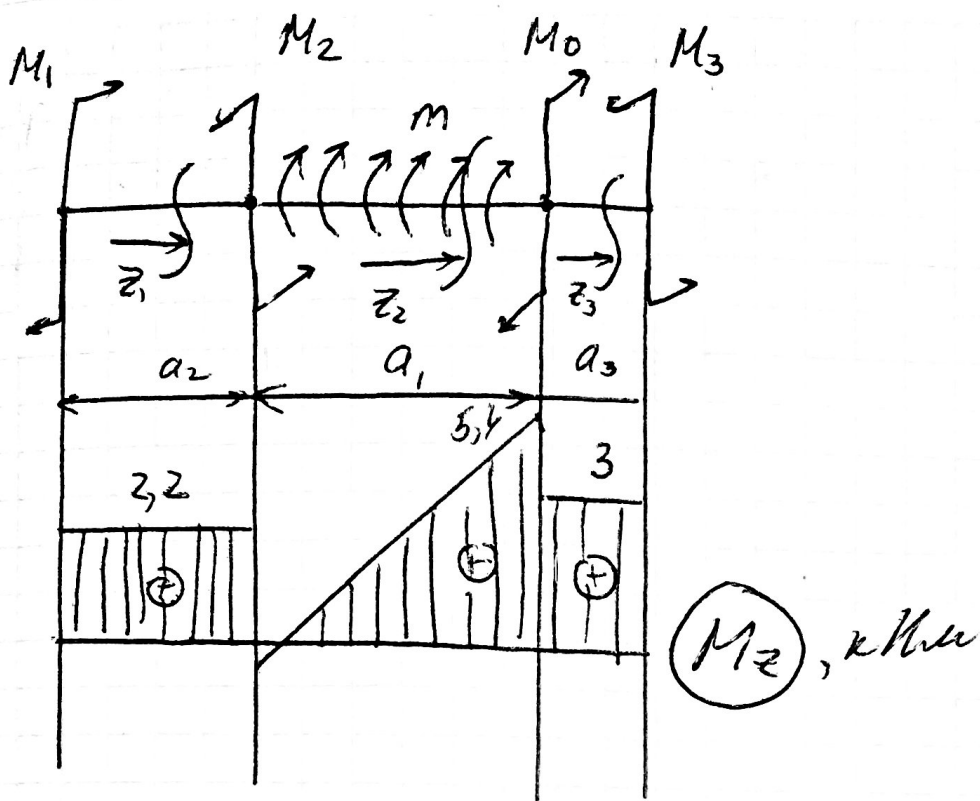
$$M_z' = M_1 = 2,2 \text{ кНм}$$

$$a_2 < z_2 < (a_1 + a_2)$$

$$M_z'' = M_1 - M_2 + m(z_2 - a_2) \Big|_{a_2}^{a_1 + a_2}$$

$$M_z''(a_2) = M_1 - M_2 = 2,2 - 2,8 = -0,6 \text{ кНм}$$

$$M_z''(a_1 + a_2) = M_1 - M_2 + m a_1 = 2,2 - 2,8 + 10 \cdot 0,6 = 5,4 \text{ кНм}$$



$$\underline{(a_2 + a_1) < z_3 < (a_1 + a_2 + a_3)}$$

$$M_2^m = M_1 - M_2 + ma_1 + M_0 = 2,2 - 2,8 + 10 \cdot 0,8 + (-2,4) = 3 \text{ kHm}$$

$$a_1 = 1,4 \text{ м}$$

$$a_2 = 1,2 \text{ м}$$

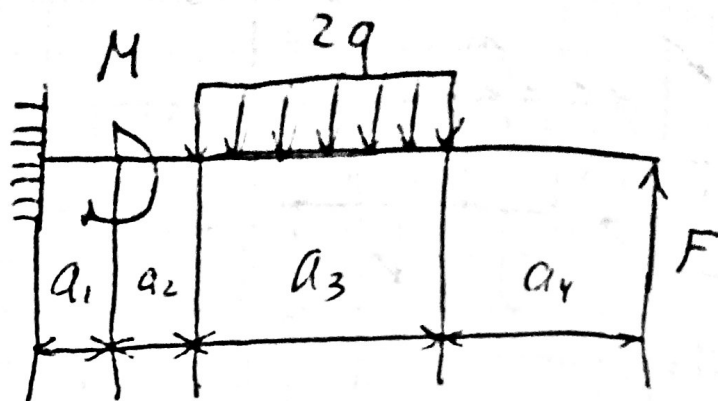
$$a_3 = 0,5 \text{ м}$$

$$a_4 = 2,3 \text{ м}$$

$$q = 20 \text{ кН/м}$$

$$F = 20 \text{ кН}$$

$$M = 35 \text{ кНм}$$



Построение эпюр ВСР

$$0 < z_1 < a_4$$

$$Q_y' = -F = -20 \text{ кН}$$

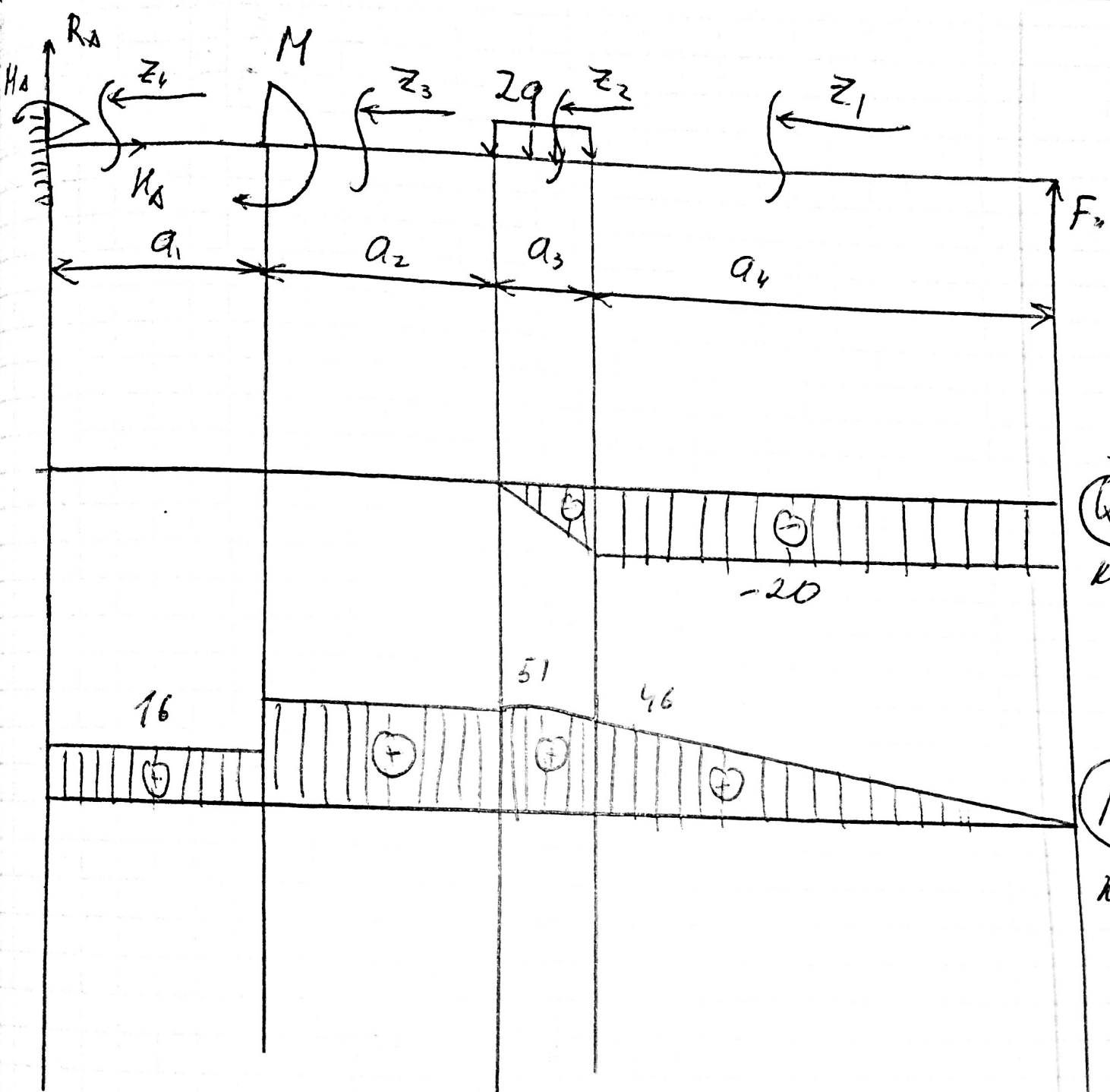
$$M_x' = F z_1 \Big|_{0 \rightarrow 0}^{a_4} \rightarrow F a_4 = 20 \cdot 2,3 = 46 \text{ кНм}$$

$$a_4 < z_2 < (a_3 + a_4)$$

$$Q_y'' = -F + 2q(z_2 - a_4) \Big|_{a_4 \rightarrow -F = -20 \text{ кН}}^{a_3 + a_4 \rightarrow -F + 2q a_3 = -20 + 2 \cdot 20 \cdot 0,5 = 0 \text{ кН}}$$

$$M_x'' = +F z_2 - 2q \frac{(z_2 - a_4)^2}{2} \Big|_{a_4 \rightarrow +F a_4 = 46 \text{ кНм}}^{a_3 + a_4}$$

$$M_x''(a_3 + a_4) = F(a_3 + a_4) - q a_3^2 = 20(0,5 + 2,3) - 20 \cdot 0,5^2 = 51 \text{ кНм}$$



$Q_y$   
 kN/m

$M_x$   
 kNm

$$\underline{(a_3 + a_4) < z_3 < (a_2 + a_3 + a_4)}$$

$$Q_y^{III} = -F + 2qa_3 = 0 \text{ kN}$$

$$M_x^{III} = Fz_3 - 2qa_3 \left( z_3 - a_4 - \frac{a_3}{2} \right) \begin{array}{l} a_3 + a_4 + a_2 \\ a_3 + a_4 \end{array}$$

$$M_x^{III}(a_3 + a_4) = F(a_3 + a_4) - 2qa_3 \left( \frac{a_3}{2} \right) =$$

$$= 20(0,5 + 2,3) - 2 \cdot 20 \cdot 0,5 \frac{0,5}{2} = 51 \text{ kNm}$$

$$M_x^{III}(a_3 + a_4 + a_2) = F(a_3 + a_4) - 2qa_3 \left( \frac{a_3}{2} + a_2 \right) =$$

$$= 20(0,5 + 2,3) - 2 \cdot 20 \cdot 0,5 \left( \frac{0,5}{2} + 1,2 \right) =$$

$$= 27 \text{ kNm}$$

$$\underline{(a_2 + a_3 + a_4) < z_4 < (a_2 + a_3 + a_4 + a_1)}$$

$$Q_y^{IV} = -F + 2qa_3 = 0 \text{ kN}$$

$$M_x^{IV} = Fz_4 - 2qa_3 \left( z_4 - a_4 - \frac{a_3}{2} \right) - M \begin{array}{l} a_2 + a_3 + a_4 + a_1 \\ a_2 + a_3 + a_4 \end{array}$$

$$M_x^{IV}(a_2 + a_3 + a_4) = F(a_2 + a_3 + a_4) - 2qa_3 \left( a_2 + \frac{a_3}{2} \right) -$$

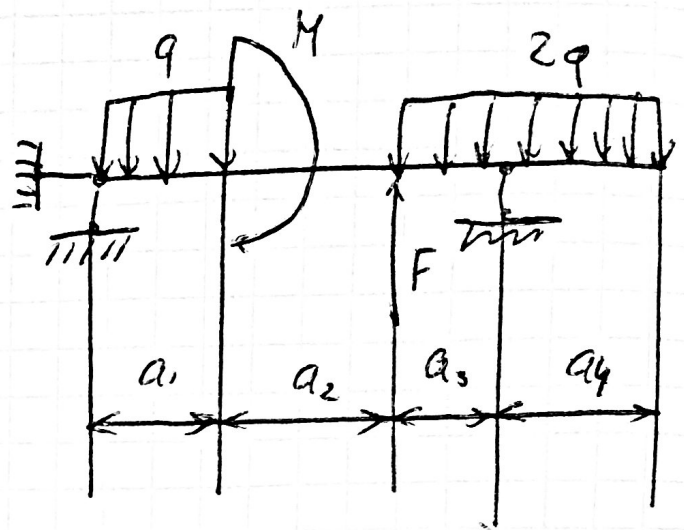
$$M = 20(1,2 + 0,5 + 2,3) - 2 \cdot 20 \cdot 0,5 \left( 1,2 + \frac{0,5}{2} \right) = 35 =$$



= 60 kWh

$$\begin{aligned} M_{\text{X}}^{\text{IV}}(a_2 + a_3 + a_4 + a_1) &= F(a_2 + a_3 + a_4 + a_1) - \\ &- 2qa_3 \left( a_2 + \frac{a_3}{2} + a_1 \right) - M = 20(1,2 + 0,5 + \\ &+ 2,3 + 1,4) - 2 \cdot 20 \cdot 0,5 \left( 1,2 + \frac{0,5}{2} + 1,4 \right) - \\ &- 35 = 60 \text{ kWh} \end{aligned}$$

$$\begin{aligned}
 a_1 &= 1,4 \text{ м} & q &= 20 \text{ кН/м} \\
 a_2 &= 1,2 \text{ м} & F &= 20 \text{ кН} \\
 a_3 &= 0,5 \text{ м} & M &= 35 \text{ кНм} \\
 a_4 &= 2,3 \text{ м}
 \end{aligned}$$



Определение опорных реакций

$$\begin{aligned}
 \sum x_i &= 0 \\
 \frac{\sum x_i}{H_A} &= 0
 \end{aligned}$$

$$\sum y_i = 0$$

$$R_A - qa_1 + F - 2q(a_3 + a_4) + R_B = 0$$

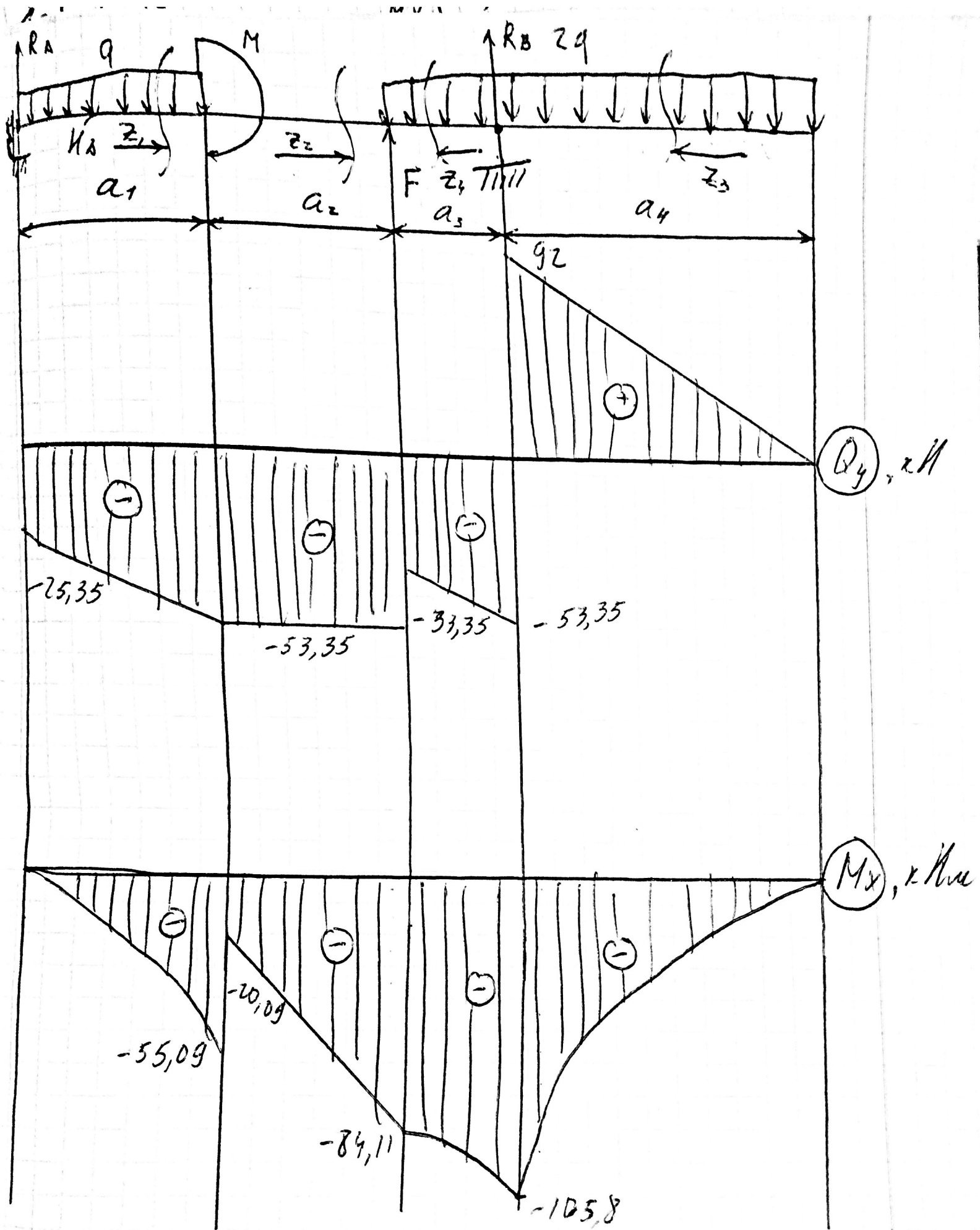
$$\sum m_A = 0$$

$$\begin{aligned}
 q \frac{a_1^2}{2} + M - F(a_1 + a_2) + 2q(a_3 + a_4) \left( a_1 + a_2 + \frac{a_3 + a_4}{2} \right) - \\
 - R_B(a_1 + a_2 + a_3) = 0
 \end{aligned}$$

$$R_B = \frac{q \frac{a_1^2}{2} + M - F(a_1 + a_2) + 2q(a_3 + a_4) \left( a_1 + a_2 + \frac{a_3 + a_4}{2} \right)}{a_1 + a_2 + a_3}$$

$$= \frac{20 \frac{1,4^2}{2} + 35 - 20(1,4 + 1,2) + 2 \cdot 20(0,5 + 2,3) \left( 1,4 + 1,2 + \frac{0,5 + 2,3}{2} \right)}{1,4 + 1,2 + 0,5}$$

$$1,4 + 1,2 + 0,5$$



$$= 145,35 \text{ кН}$$

$$R_A = qa_1 - F + 2q(a_3 + a_4) - R_B = 20 \cdot 1,4 -$$

$$- 20 + 2 \cdot 20(0,5 + 2,3) = 145,35 = -25,35 \text{ кН}$$

Полное уравнение  $\Rightarrow$   $Q_y$ ,  $M_x$

$$0 < z_1 < a_1$$

$$Q_y' = R_A - qz_1 \left| \begin{array}{l} a_1 \rightarrow R_A - qa_1 = -25,35 - 20 \cdot 1,4 = -53,35 \text{ кН} \\ 0 \rightarrow R_A = -25,35 \text{ кН} \end{array} \right.$$

$$M_x' = R_A z_1 - q \frac{z_1^2}{2} \Big|_0^{a_1}$$

$$M_x'(0) = 0$$

$$M_x'(a_1) = R_A a_1 - q \frac{a_1^2}{2} = -25,35 \cdot 1,4 - 20 \frac{1,4^2}{2} = -55,09 \text{ кНм}$$

$$a_1 < z_2 < (a_1 + a_2)$$

$$Q_y'' = R_A - qa_1 = -53,35 \text{ кН}$$

$$M_x'' = R_A z_2 - qa_1(z_2 - \frac{a_1}{2}) - M \Big|_{a_1}^{a_1 + a_2}$$

$$M_x''(a_1) = R_A a_1 - qa_1 \frac{a_1}{2} = M = -55,09 + 35 = -20,09 \text{ кНм}$$

$$M_x''(a_1 + a_2) = R_A(a_1 + a_2) - qa_1(a_2 + \frac{a_1}{2}) - M =$$

$$= -25,35(1,4 + 1,2) - 20 \cdot 1,4(1,2 + \frac{1,4}{2}) + 35 = -84,11 \text{ кНм}$$

$$0 < z_3 < a_4$$

$$Q_y^{III} = 2q z_3 \left| \begin{array}{l} a_4 \rightarrow 2qa_4 = 2 \cdot 20 \cdot 2,3 = 92 \text{ kN} \\ 0 \rightarrow 0 \end{array} \right.$$

$$M_x^{III} = -2q \frac{z_3^2}{2} \left| \begin{array}{l} a_4 \rightarrow -qa_4^2 = -20 \cdot 2,3^2 = -105,8 \text{ kNm} \\ 0 \rightarrow 0 \end{array} \right.$$

$$a_4 < z_4 < (a_3 + a_4)$$

$$Q_y^{IV} = 2qa_4 - R_B + 2q(z_4 - a_4) \left| \begin{array}{l} a_3 + a_4 \\ a_4 \end{array} \right.$$

$$Q_y^{IV}(a_4) = 2qa_4 - R_B = 2 \cdot 20 \cdot 2,3 - 145,35 = -53,35 \text{ kN}$$

$$Q_y^{IV}(a_3 + a_4) = 2qa_4 - R_B + 2qa_3 = -53,35 + 2 \cdot 20 \cdot 0,5 = -33,35 \text{ kN}$$

$$M_x^{IV} = -2q \frac{z_4^2}{2} + R_B(z_4 - a_4) \left| \begin{array}{l} a_3 + a_4 \\ a_4 \end{array} \right.$$

$$M_x^{IV}(a_4) = -qa_4^2 = -105,8 \text{ kNm}$$

$$M_x^{IV}(a_4 + a_3) = -q(a_4 + a_3)^2 + R_B a_3 = -20(2,3 + 0,5)^2 + 145,35 \cdot 0,5 = -84,1 \text{ kNm}$$

$$l_1 = 1 \mu$$

$$l_2 = 1,4 \mu$$

$$l_3 = 1,1 \mu$$

$$a_4 = 0,8 \mu$$

$$a_2 = 2a_3 = 1,3 \mu$$

$$F_1 = 40 \text{ kN}$$

$$F_2 = 20 \text{ kN}$$

$$F_3 = 30 \text{ kN}$$

$$\sigma_T = 850 \text{ MPa}$$

$$q = 40 \text{ kN}/\mu \quad n_T = 1,3 ; \text{ max } 45^\circ$$

$$0 < \underline{I} < (L_1 + L_2 + L_3 - a_1 - a_2 - a_3)$$

$$N_z' = -q z_1 \Big|_0^{(L_1 + L_2 + L_3 - a_1 - a_2 - a_3)} =$$

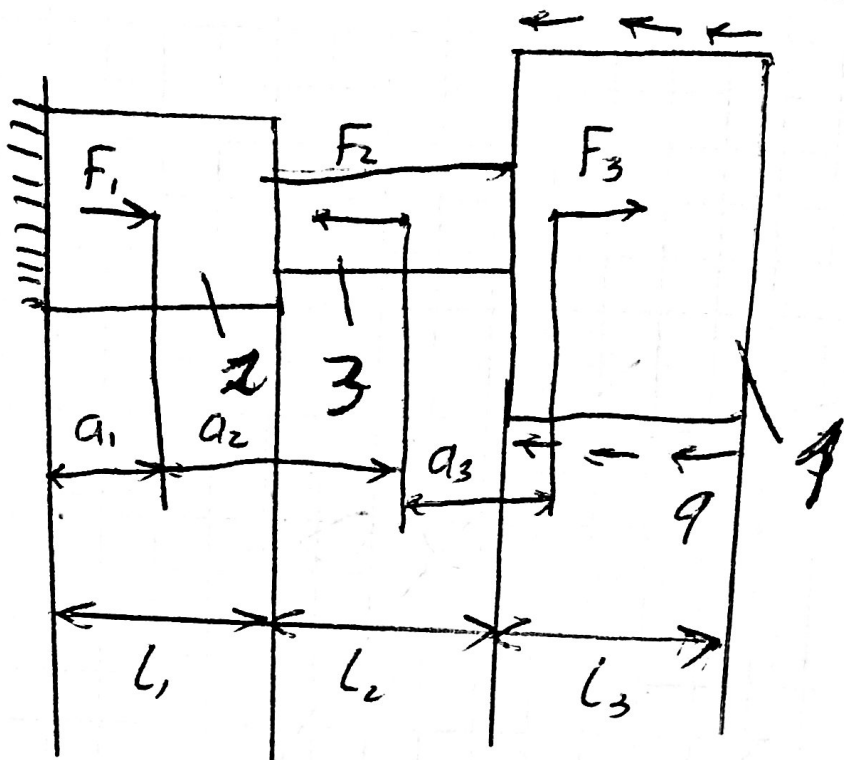
$$N_z'(L_1 + L_2 + L_3 - a_1 - a_2 - a_3) = -q(L_1 + L_2 + L_3 - a_1 - a_2 - a_3) =$$

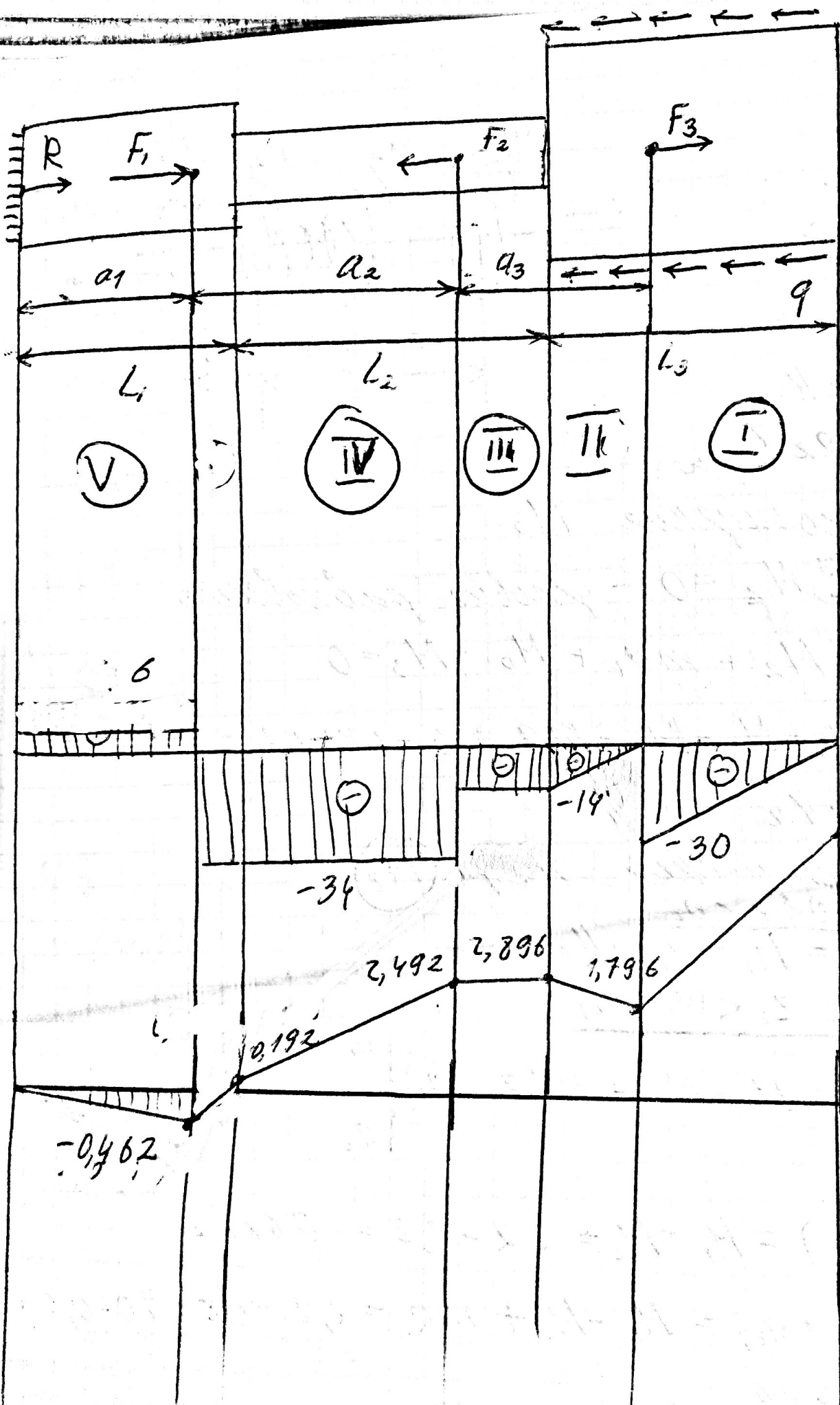
$$= -40(1 + 1,4 + 1,1 - 0,8 - 1,3 - \frac{1,3}{2}) = -30 \text{ kN}$$

$$(L_1 + L_2 + L_3 - a_1 - a_2 - a_3) < \underline{II} < (L_3)$$

$$N_z'' = -q z_2 + F_3 \Big|_{L_1 + L_2 + L_3 - a_1 - a_2 - a_3}^{L_3}$$

$$N_z''(L_1 + L_2 + L_3 - a_1 - a_2 - a_3) = -q(L_1 + L_2 + L_3 - a_1 - a_2 - a_3) +$$





$N_z, \text{kN}$

5,296

$\Delta, \text{mm}$

Определение напряемения

$$0 < \textcircled{I} < (l_1 + l_2 + l_3 - a_1 - a_2 - a_3)$$

$$\sigma_z' = \frac{N_z'}{A_1} = \frac{-q z_1}{A_1} \left| \begin{array}{l} l_1 + l_2 + l_3 - a_1 - a_2 - a_3 \\ 0 \rightarrow 0 \end{array} \right.$$

$$\begin{aligned} \sigma_z' (l_1 + l_2 + l_3 - a_1 - a_2 - a_3) &= \frac{-q (l_1 + l_2 + l_3 - a_1 - a_2 - a_3)}{A_1} \\ &= \frac{-40 (1 + 1,4 + 1,1 - 0,8 - 1,3 - \frac{1,3}{2})}{A_1} \cdot 10^3 = \frac{-30000}{A_1} \end{aligned}$$

$$(l_1 + l_2 + l_3 - a_1 - a_2 - a_3) < \textcircled{II} < l_3$$

$$\sigma_z'' = \frac{N_z''}{A_1} = \frac{-q z_2 + F_3}{A_1} \left| \begin{array}{l} l_3 \\ l_3 + l_1 + l_2 - a_1 - a_2 - a_3 \end{array} \right.$$

$$\begin{aligned} \sigma_z'' (l_3 + l_1 + l_2 - a_1 - a_2 - a_3) &= \frac{-q (l_3 + l_1 + l_2 - a_1 - a_2 - a_3)}{A_1} + \frac{F_3}{A_3} \\ &= \left( \frac{-40 (1,1 + 1 + 1,4 - 0,8 - 1,3 - \frac{1,3}{2})}{A_1} + \frac{30}{A_3} \right) \cdot 10^3 = \\ &= 0 \end{aligned}$$

$$\sigma_z'' (l_3) = \frac{-q l_3 + F_3}{A_1} = \frac{-40 \cdot 1,1 + 30}{A_1} \cdot 10^3 = \frac{-14000}{A_1}$$



$$L_3 < \textcircled{\text{III}} < (L_1 + L_2 - a_1 - a_2)$$

$$\sigma_z^{\text{III}} = \frac{N_z^{\text{III}}}{A_3} = \frac{-qL_3 + F_3}{A_3} = \frac{-40 \cdot 1,1 + 30}{A_3} \cdot 10^3 =$$
$$= \frac{-14000}{A_3}$$

$$(L_1 + L_2 - a_1 - a_2) < \textcircled{\text{IV}} < L_2 + L_3$$

$$\sigma_z^{\text{IV}} = \frac{-qL_3 + F_3 - F_2}{A_3} = \frac{-40 \cdot 1,1 + 30 - 20}{A_3} \cdot 10^3 =$$
$$= \frac{-34000}{A_3}$$

$$L_2 + L_3 < \textcircled{\text{V}} < L_1 + L_2 + L_3 - a_1$$

$$\sigma_z^{\text{V}} = \frac{-qL_3 + F_3 - F_2}{A_2} = \frac{-34000}{A_2}$$

$$(L_1 + L_2 + L_3 - a_1) < \textcircled{\text{VI}} < L_1 + L_2 + L_3$$

$$\sigma_z^{\text{VI}} = \frac{-qL_3 + F_3 - F_2 + F_1}{A_2} = \frac{-40 \cdot 1,1 + 30 - 20 + 40}{A_2} \cdot 10^3 =$$
$$= \frac{14000}{A_2}$$

Определение ~~из~~ прочности стержня А

$$\sigma_{\max} \leq [\sigma]$$

$$\sigma_{\max} \leq \frac{\sigma_T}{n_T}$$

1-й уравнение

или

$$\frac{30000}{A_1} \leq \frac{\sigma_T}{n_T}$$

$$A_1 \geq \frac{30000 n_T}{\sigma_T} = \frac{30000 \cdot 1,3}{850 \cdot 10^6} = 46 \cdot 10^{-6} \text{ м}^2$$

2-й уравнение

$$\frac{34000}{A_2} \leq \frac{\sigma_T}{n_T}$$

$$A_2 \geq \frac{34000 n_T}{\sigma_T} = \frac{34000 \cdot 1,3}{850 \cdot 10^6} = 52 \cdot 10^{-6} \text{ м}^2$$

3-й уравнение

$$A_3 \geq \frac{34000 n_T}{\sigma_T} = 52 \cdot 10^{-6} \text{ м}^2$$

Прямая  $\Rightarrow$   $\Sigma N_i = 0$

$$\Sigma N_i = 0$$

$$R + F_1 - F_2 + F_3 - qL_3 = 0$$

$$R = qL_3 - F_3 + F_2 - F_1 = 40 \cdot 1,1 - 30 + 20 - 40 = -6 \text{ кН}$$

$$0 < \textcircled{V} < a_1$$

$$\Delta_1 = \frac{R}{EA_2} a_1 = \frac{-6 \cdot 10^3 \cdot 0,8}{2 \cdot 10^{11} \cdot 52 \cdot 10^{-6}} = -462 \cdot 10^{-6} \text{ м}$$

$$= -0,462 \text{ мм}$$

$$a_1 < \textcircled{V} < L_1$$

$$\Delta_2 = \frac{R + F_1}{EA_2} (L_1 - a_1) = \frac{-6 \cdot 10^3 + 40 \cdot 10^3}{2 \cdot 10^{11} \cdot 52 \cdot 10^{-6}} (1 - 0,8) =$$

$$= 654 \cdot 10^{-6} \text{ м} = 0,654 \text{ мм}$$

$$\Delta_{II} = \Delta_1 + \Delta_2 = -0,462 + 0,654 = \underline{0,192 \text{ мм}}$$

$$L_1 < \textcircled{IV} < (a_1 + a_2)$$

$$\Delta_3 = \frac{R + F_1}{EA_3} (-L_2 + a_1 + a_2) = \frac{-6 \cdot 10^3 + 40 \cdot 10^3}{2 \cdot 10^{11} \cdot 52 \cdot 10^{-6}} (-1,4 + 0,8 +$$

$$+ 1,3) = 0,0023 \text{ м} = 2,3 \text{ мм}$$

$$\Delta_{III} = 0,192 + 2,3 = \underline{2,492 \text{ мм}}$$

$$\underline{(a_1 + a_2) < (II) < (L_1 + L_2)}$$

$$\Delta_4 = \frac{R + F_1 - F_2}{EA_3} (L_1 + L_2 - a_1 - a_2) = \frac{(-6 \cdot 10^3 + 40 \cdot 10^3 - 20 \cdot 10^3)}{2 \cdot 10^{11} \cdot 52 \cdot 10^{-6}}$$

$$\cdot (1 + 1,4 - 0,8 - 1,3) = 404 \cdot 10^{-6} \mu = 0,404 \text{ mm}$$

$$\Delta_{IV} = \Delta_{III} + \Delta_4 = 2,492 + 0,404 = \underline{2,896 \text{ mm}}$$

$$\underline{(L_1 + L_2) < (II) < (a_1 + a_2 + a_3)}$$

$$\Delta_5 = \int_z \frac{R + F_1 - F_2 - q(z - L_1 - L_2)}{EA_1} dz =$$

$$= (R + F_1 - F_2)(a_1 + a_2 + a_3) - q \frac{(a_1 + a_2 + a_3 - L_1 - L_2)^2}{2}$$

$$= \frac{(R + F_1 - F_2)(L_1 + L_2)}{EA_1} = \frac{(-6 \cdot 10^3 + 40 \cdot 10^3 - 20 \cdot 10^3)}{2 \cdot 10^{11} \cdot 46 \cdot 10^{-6}} \cdot (0,8 + 1,3 + \frac{1,3}{2} - 1 - 1,4)$$

$$= \frac{40 \cdot 10^3 (0,8 + 1,3 + \frac{1,3}{2} - 1 - 1,4)^2}{2 \cdot 2 \cdot 10^{11} \cdot 46 \cdot 10^{-6}} = -0,0011 \text{ mm}$$

$$= -1,1 \text{ mm}$$

$$\Delta_V = \Delta_{IV} + \Delta_S = 2,896 - 1,1 = \underline{1,796 \mu\text{m}}$$

$$(a_1 + a_2 + a_3) < \textcircled{I} < (L_1 + L_2 + L_3)$$

$$\Delta_6 = \int_z \frac{R + F_1 - F_2 + F_3 - q(z_6 - L_1 - L_2)}{EA_1} dz =$$

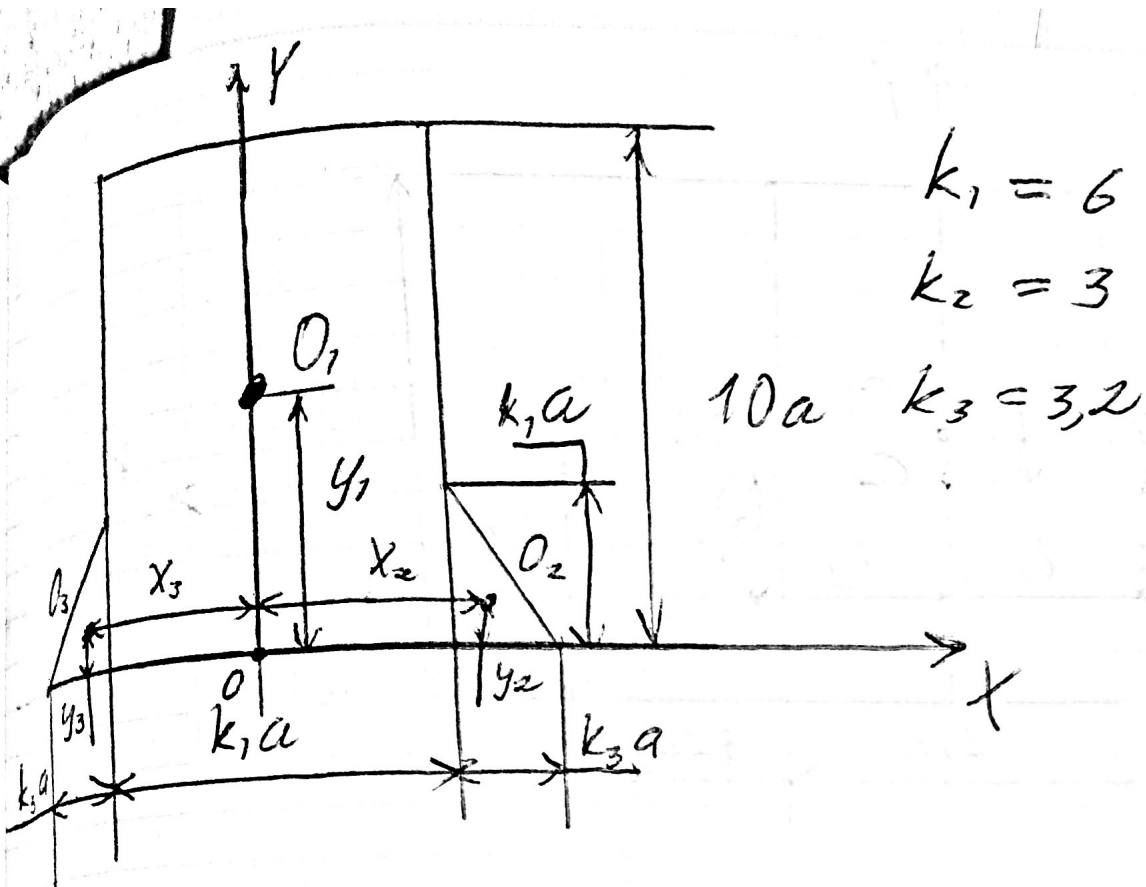
$$= \frac{(R + F_1 - F_2 + F_3)(L_1 + L_2 + L_3 - a_1 - a_2 - a_3)}{EA_1} -$$

$$- \frac{q(L_3 - (a_1 + a_2 + a_3 - L_1 - L_2))^2}{2EA_1} =$$

$$= \frac{(-6 \cdot 10^3 + 40 \cdot 10^3 - 20 \cdot 10^3 + 30 \cdot 10^3)(1 + 1,4 + 1,1 - 0,8 - 1,3 - \frac{1,3}{2})}{2 \cdot 10^{11} \cdot 46 \cdot 10^{-6}}$$

$$- \frac{40 \cdot 10^3 \left(1,1 - 0,8 - 1,3 - \frac{1,3}{2} + 1 + 1,4\right)^2}{2 \cdot 2 \cdot 10^{11} \cdot 46 \cdot 10^{-6}} = 0,0035 \mu\text{m} = 3,5 \mu\text{m}$$

$$\Delta_{V1} = \Delta_V + \Delta_6 = 1,796 + \cancel{0,0035} 3,5 = \underline{5,296 \mu\text{m}}$$



Onpreghesence ystampa mammetta

$$x_c = \frac{\sum A_i x_i}{\sum A_i} = \frac{A_1 x_1 + A_2 x_2 + A_3 x_3}{A_1 + A_2 + A_3} =$$

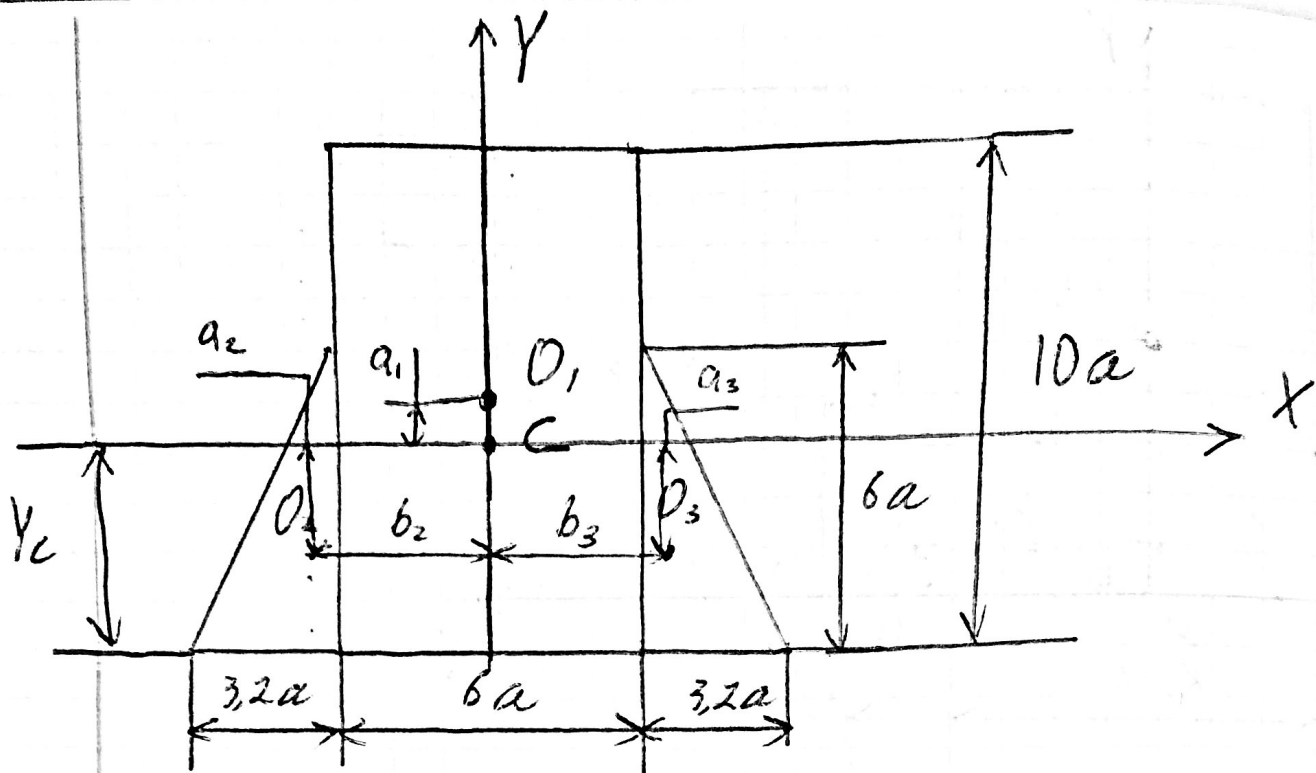
$$= \frac{0 + A_2 x_2 + A_2 (-x_2)}{A_1 + 2A_2} = 0$$

$$y_c = \frac{\sum A_i y_i}{\sum A_i} = \frac{A_1 y_1 + A_2 y_2 + A_3 y_3}{A_1 + A_2 + A_3} =$$

$$= \frac{A_1 y_1 + A_2 y_2 + A_2 (-y_2)}{A_1 + 2A_2} = \frac{A_1 y_1}{A_1 + 2A_2}$$

$$A_1 = 10a \cdot 6a = 60a^2$$

$$y_1 = \frac{10a}{2} = 5a$$



$$y_c \quad A_2 = A_3 = \frac{6a \cdot 3,2a}{2} = 9,4a^2$$

$$y_c = \frac{60a^2 \cdot 5a}{60a^2 + 9,4a^2} = 4,32a$$

Определим центральные моменты инерции

$$J_{x_1} = \frac{bh^3}{12} = \frac{6a \cdot (10a)^3}{12} = 500a^4$$

$$J_{y_1} = \frac{hb^3}{12} = \frac{10a \cdot (6a)^3}{12} = 180a^4$$

$$a_1 = \frac{10a}{2} - 4,32a = 1,32a$$

$$a_2 = a_3 = 4,32a - \frac{1}{3} \cdot 6a = 2,32a$$

$$b_2 = b_3 = \frac{6a}{2} + \frac{1}{3} \cdot 3,2a = 4,07a$$

$$J_{x_2} = J_{x_3} = \frac{bh^3}{36} = \frac{3,2a \cdot (6a)^3}{36} = 19,2a^4$$

$$J_{y_2} = J_{y_3} = \frac{hb^3}{36} = \frac{6a \cdot (3,2a)^3}{36} = 5,46a^4$$

$$J_x = J_x' + J_x'' + J_x''' = (J_{x_1} + a_1^2 \Lambda_1) + (J_{x_2} + a_2^2 \Lambda_2) + (J_{x_3} + a_3^2 \Lambda_3) = (J_{x_1} + a_1^2 \Lambda_1) + 2(J_{x_2} + a_2^2 \Lambda_2) =$$

$$(\cancel{500}a^4 + (1,32a)^2 \cdot 60a^2) + 2(19,2a^4 + (2,32a)^2 \cdot 9,4a^2) =$$

$$= \underline{\underline{7'44,13 a^4}}$$

$$J_y = J_y' + J_y'' + J_y''' = J_{y_1} + (J_{y_2} + b_2^2 \Lambda_2) +$$

$$+ (J_{y_3} + b_3^2 \Lambda_3) = J_{y_1} + 2(J_{y_2} + b_2^2 \Lambda_2) =$$

$$= 180a^4 + 2(5,46a + (4,07a)^2 \cdot 9,4a) = \underline{\underline{502,34a^4}}$$